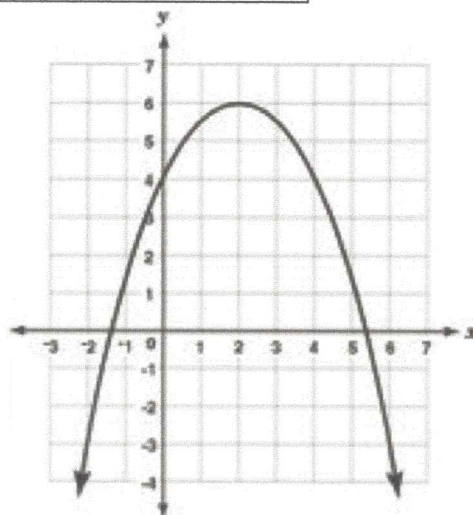


Name:

Solutions

I. Shown is the graph of $y = g(x)$



1. Evaluate:

a. $g(0) = 4$

b. $g(6) = -3$

2. Write the domain and range of the function using interval notation.

$D: (-\infty, \infty)$

$R: (-\infty, 6]$

3. State the interval(s) on which the function is:

a. increasing

$(-\infty, 2]$

b. decreasing

$[2, \infty)$

c. constant

N/A

4. State the interval(s) for which:

a. $g(x) > 0$

$(-1.4, 5.4)$

b. $g(x) < 0$

$(-\infty, -1.4) \cup (5.4, \infty)$

5. State each value:

a. the maximum value of $y = g(x)$

$y = 6$

b. the minimum value of $y = g(x)$

N/A

6. Solve $g(x) = 4$, i.e. for what value(s) of x does $g(x) = 4$ hold true?

$x = 0$ and $x = 4$

7. State the coordinates of each (approximate if necessary):

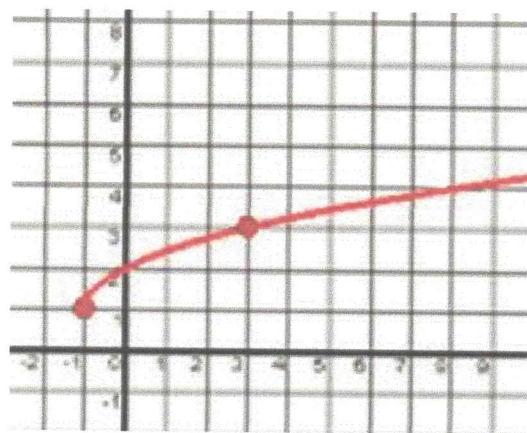
a. any x-intercepts

$\approx (-1.4, 0)$

b. the y-intercept

$(0, 4)$

II. Shown is the graph of $y = f(x)$



1. Evaluate:

a. $f(0) = 2$

b. $f(8) = 4$

2. Write the domain and range of the function using interval notation.

$D: [-1, \infty)$

$R: [1, \infty)$

3. State the interval(s) on which the function is:

a. increasing

$[-1, \infty)$

b. decreasing

N/A

c. constant

N/A

4. State the interval(s) for which:

a. $f(x) > 0$

$[-1, \infty)$

b. $f(x) < 0$

N/A

5. State each value:

a. the maximum value of $y = f(x)$

N/A

b. the minimum value of $y = f(x)$

$y = 1$

6. Solve $f(x) = 1$

$x = -1$

7. State the coordinates of each:

a. any x-intercepts

N/A

b. the y-intercept

$(0, 2)$

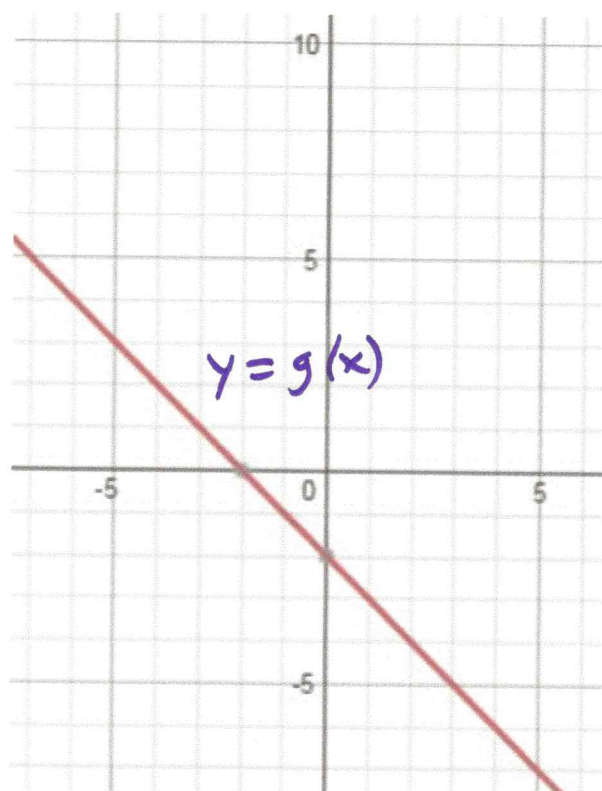
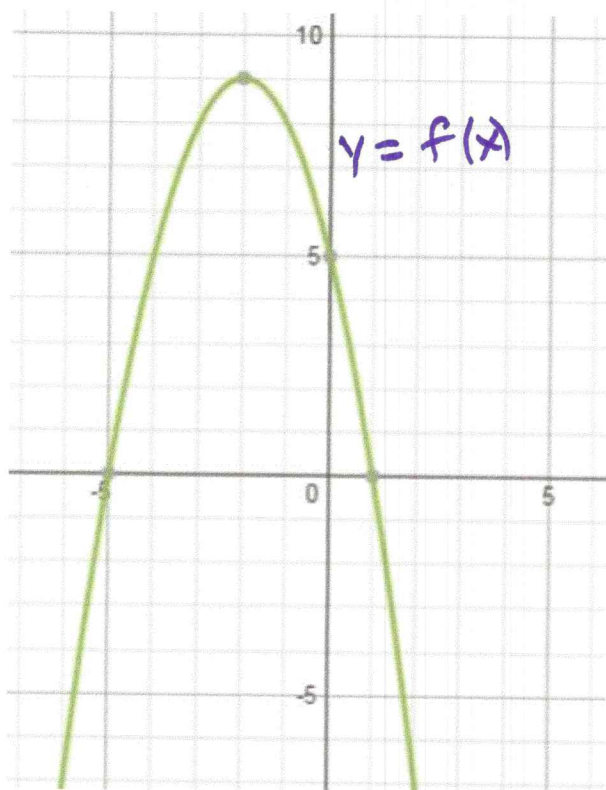
8. Is the graph concave up or concave down?

concave down on the interval $[-1, \infty)$

III. Given the two functions $f(x) = x - 4$ and $g(x) = 2 - x^2$:

<p>1. Evaluate $(f+g)(x)$</p> $\begin{aligned} x-4 + 2-x^2 \\ x-2-x^2 \\ -x^2+x-2 \end{aligned}$	<p>2. Evaluate $(g-f)(x)$</p> $\begin{aligned} 2-x^2 - (x-4) \\ 2-x^2-x+4 \\ -x^2-x+6 \end{aligned}$
<p>3. Evaluate $(fg)(x)$</p> $\begin{aligned} (x-4)(2-x^2) \\ 2x-x^3-8+4x^2 \\ -x^3+4x^2+2x-8 \end{aligned}$	<p>4. Evaluate $\left(\frac{f}{g}\right)(x)$</p> $\frac{x-4}{2-x^2}$
<p>5. Evaluate $f(g(x))$</p> $\begin{aligned} f(2-x^2) \\ 2-x^2-4 \\ -x^2-2 \end{aligned}$	<p>6. Evaluate $(g \circ f)(x) = g(f(x))$</p> $\begin{aligned} g(x-4) &= 2-(x-4)^2 \\ &= 2-(x^2-8x+16) \\ &= 2-x^2+8x-16 \\ &= -x^2+8x-14 \end{aligned}$
<p>7. Evaluate $(f \circ f)(x) = f(f(x))$</p> $\begin{aligned} f(x-4) &= (x-4)-4 \\ &= x-8 \end{aligned}$	<p>8. Evaluate $f(3) \cdot g(3)$</p> $\begin{aligned} (3-4)(3-4) \\ (-1)(-1) \\ 1 \end{aligned}$
<p>9. Evaluate $f(g(-1)) = f(2-(1)^2)$</p> $\begin{aligned} f(2-1) &= f(1) = 1-4 \\ &= -3 \end{aligned}$	<p>10. Evaluate $(g \circ f)(8) = g(f(8))$</p> $\begin{aligned} g(8-4) &= g(4) = 2-4^2 \\ &= 2-16 = -14 \end{aligned}$
<p>11. State the domain and range of $f(g(x))$</p> $\begin{aligned} f(2-x^2) &= 2-x^2-4 \\ &= -x^2-2 \quad V(0, -2) \\ D: (-\infty, \infty) \quad R: (-\infty, -2] \end{aligned}$	<p>12. State the domain and range of $g(f(x))$</p> <p>from #6 $g(f(x)) = -x^2+8x-14$</p> $\begin{aligned} V(4, 2) \\ D: (-\infty, \infty) \quad R: (-\infty, 2] \end{aligned}$

IV. Use the graphs of $y = f(x)$ on the left and $y = g(x)$ on the right below to answer # 13 - 22



1. Evaluate $(f+g)(0) = f(0) + g(0)$ $= 5 + -2 = 3$	2. Evaluate $(g \circ f)(0) = $ $f(0)$ $= g(f(0)) = g(5) = -7$
3. Evaluate $f(-1) - g(-1)$ $9 - -1$	4. Evaluate $(f \circ g)(-4) = f(g(-4))$ $f(2) = -7$
5. Evaluate $f(g(-2)) = f(0) = 5$	6. Evaluate $g(g(3)) = g(-5) = 3$
7. Evaluate $f(-3) \cdot g(-3)$ $0 \cdot 1$ 0	8. Evaluate $f(0) \cdot g(0) = 5 \cdot (-2) = -10$
9. Evaluate $\left(\frac{f}{g}\right)(1) = \frac{f(1)}{g(1)} = \frac{0}{-3}$ $= 0$	10. Evaluate $(g-f)(-2) = g(-2) - f(-2)$ $= 0 - 9 = -9$